

$$m_{\text{zon}} := 1.98 \cdot 10^{30} \quad G := 6.67 \cdot 10^{-11} \quad c := 3 \cdot 10^8 \quad r_{\text{zon}} := 680 \cdot 10^6$$

$$g(r) := \frac{m_{\text{zon}} \cdot G}{r^2}$$

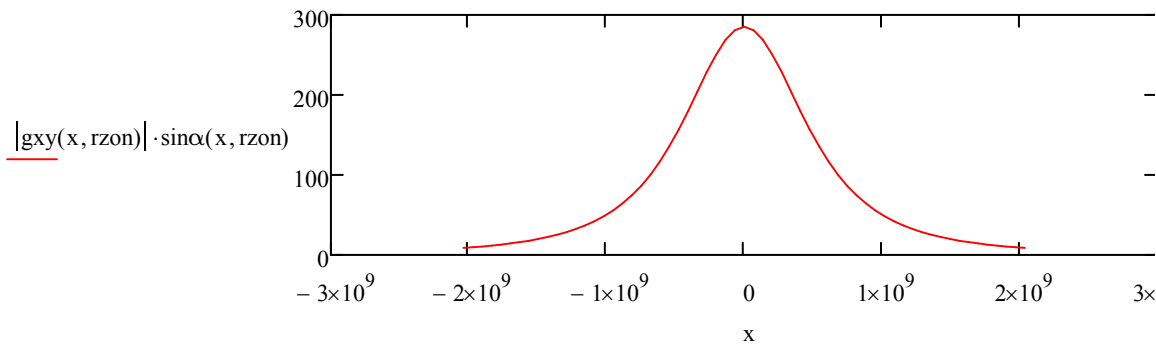
$$g(r_{\text{zon}}) = 285.61$$

$$g_{\text{alpha_r}}(\alpha, r_{\text{zon}}) := \begin{pmatrix} \frac{m_{\text{zon}} \cdot G}{r_{\text{zon}}^2} \cdot \sin(\alpha) \\ \frac{m_{\text{zon}} \cdot G}{r_{\text{zon}}^2} \cdot \cos(\alpha) \end{pmatrix}$$

$$\sin \alpha(x, r_{\text{zon}}) := \sqrt{\frac{r_{\text{zon}}^2}{x^2 + r_{\text{zon}}^2}} \quad \cos \alpha(x, r_{\text{zon}}) := \sqrt{\frac{x^2}{x^2 + r_{\text{zon}}^2}}$$

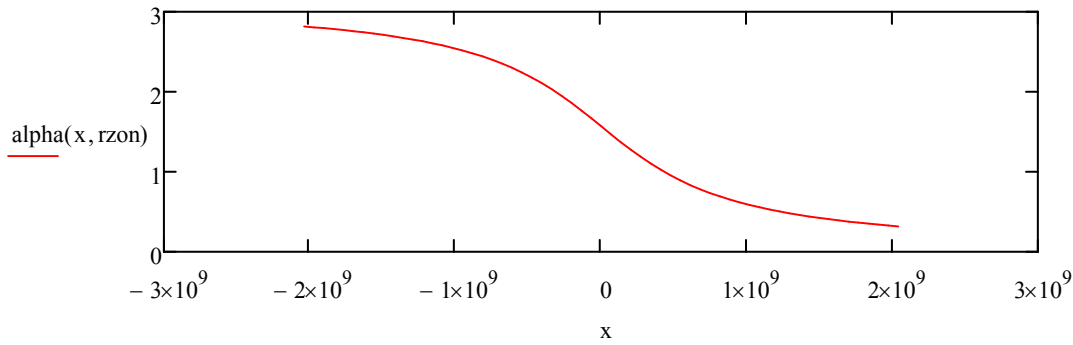
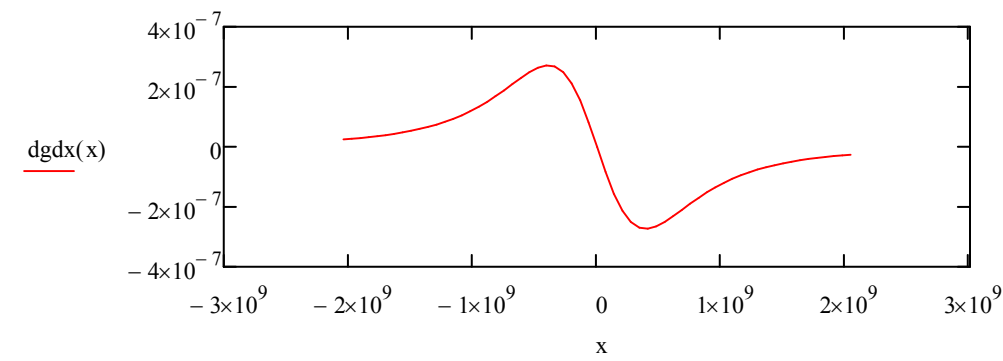
$$g_{xy}(x, r_{\text{zon}}) := \begin{bmatrix} \frac{m_{\text{zon}} \cdot G}{x^2 + r_{\text{zon}}^2} \cdot \sqrt{\frac{r_{\text{zon}}^2}{(x^2 + r_{\text{zon}}^2)}} \\ \frac{m_{\text{zon}} \cdot G}{x^2 + r_{\text{zon}}^2} \cdot \sqrt{\frac{x^2}{(x^2 + r_{\text{zon}}^2)}} \end{bmatrix}$$

$$x := -3 \cdot r_{\text{zon}}, -2.9 \cdot r_{\text{zon}} .. 3 \cdot r_{\text{zon}}$$

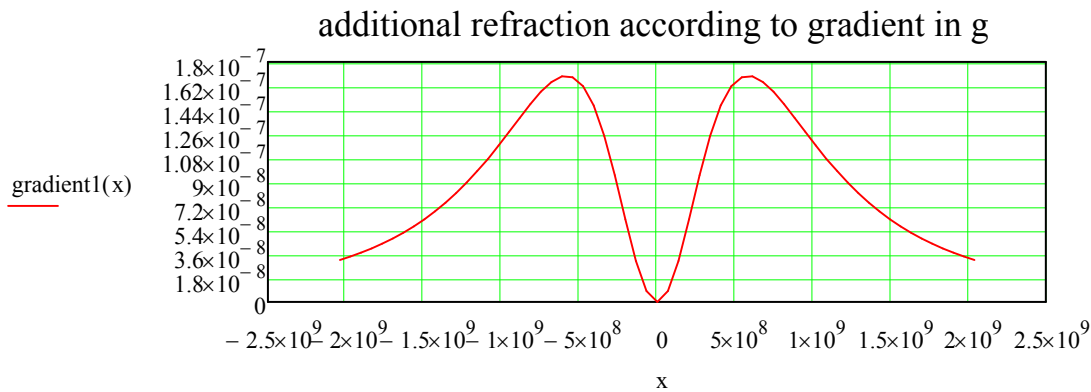


$$\alpha(x, r) := \arccos\left(\frac{x}{\sqrt{x^2 + r_{\text{zon}}^2}}\right)$$

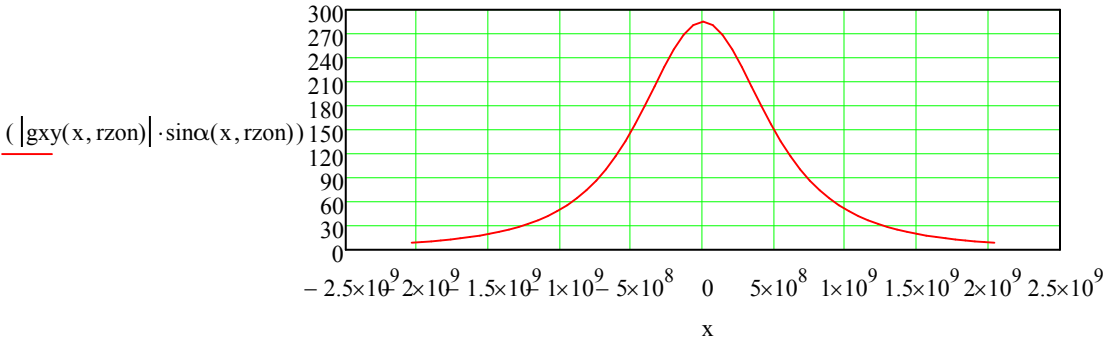
$$\text{dgd}x(x) := \frac{d}{dx} |g_{xy}(x, r_{zon})|$$



$$\text{gradient1}(x) := \text{dgd}x(x) \cdot \left(\alpha(x, r_{zon}) - \frac{\pi}{2} \right)$$



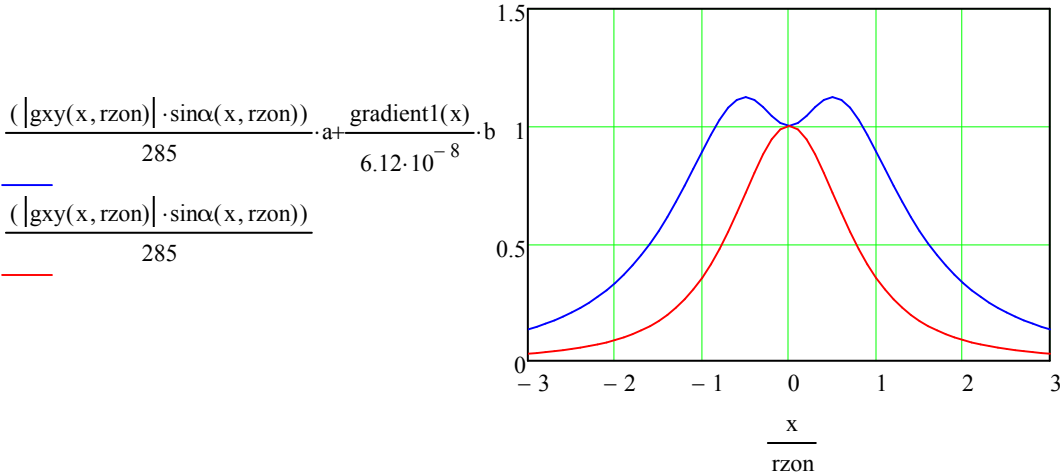
refraction according to equivalence principle



a := 1

b := 0.2

total refraction



10⁹